

Neural Networks as Radial-Interval Systems through Learning Function

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Abstract— This paper presents a novel dimension of neural networks through the approach of interval systems for great more forecasting activity. The artificial neural network (ANN) based models are the most popular ones for load forecasting and other applications. This approach is only a thought line that can enhance the fundamental requirement of all networks giving and incorporating the analytical and expertise knowledge in forecasting from the existential approaches. [1] Interval systems as an approach to approximate interval models by neural networks is proposed.

Keywords— MLP, RBFNN, Interval Systems.

I. INTRODUCTION

An enormous upwelling of interest has grown in recent years in application of neural networks to industrial processes. Their advantage is that no complex mathematical formulation or quantitative correlation between inputs and outputs is required. [2] Many years' data are also not necessary. The effective performance of Neural networks [3,4,5] in the context of ill-defined processes has led to successful application in forecasting procedures. As a consequence, pattern recognition [6], expert systems [7,8] and neural networks [9,17] have been proposed for electric load forecasting. Expert system based methods capture the expert knowledge into a comprehensive database, which is then used for predicting the future load. These models exploit knowledge of human experts for the development of rules for forecasting. However, transformation of an expert knowledge to a set of mathematical rules is often a very difficult task. In this aspect a quantitative analysis termed knowledge can uplift our work of forecasting.

II. RELATED WORK

The literature study behind this is purely a analytical way of incorporating the inputs of multilayer perceptron into the defined structured method called interval systems. Radial basis functions networks are networks, which features the architecture of the instar-out star model and uses the hybrid unsupervised and supervised learning scheme, is the RBFN suggested by Moody and Darken [2]. The RBFN is designed to perform input-output mapping trained by examples (x_k, d_k) , $k=1, 2, \dots, p$. The RBFN is based on the concept of the locally tuned and overlapping receptive field structure, studied in the cerebral cortex, the visual cortex, etc. Unlike the instar-out star model, in which the hidden nodes are of linear winner-take-all-nodes type, the RBFN hidden nodes follow a normalized Gaussian activation function:

$$zq_gq(x) = \exp[-\sum_{j=1}^m (x_j - m_{qj})^2 / 2s_{qj}^2]$$

$$Rk(x) = \exp[-\sum_{j=1}^m (x_j - m_{kj})^2 / 2s_{kj}^2]$$

Where x is the input vector. Thus, the hidden node q gives a maximum response to input vectors close to m_q . Each hidden node q is said to have its own receptive field $R_q(x)$ in the input

space, which is a region centred on m_q with size proportional to s_q , where m_q and s_q are the mean (an m -dimensional vector) and variance of the q th Gaussian function, respectively. Gaussian functions are a particular example of radial basis functions.

The output of the RBFN is simply the hidden node output weighted sum:

$$y_i = \sum_{q=1}^n w_{iq} zq_gq(x)$$

$$w_{iq} = \sum_{k=1}^p d_k Rk(x)$$

where $ai(_)$ is the output activation function and ui is the threshold value. Generally, $ai(_)$ is an identity function (i.e. the output node is a linear unit) and $ui=0$. The present work adopts a systematic approach to the problem of centre selection. Because a fixed centre corresponds to a given regressor in a linear regression model, the selection of RBF centres can be regarded as a problem of subset selection. The orthogonal least squares method can be employed as a forward selection procedure, which constructs RBFN in a rational way. [14,15]

The process goes like choosing the appropriate RBF centres one by one from taken training data points until a satisfactory network is obtained. Each selected centre minimizes the increment to the desired output variance, thus ill-conditioned problems; the frequent happening can stop the recurrence. In contrast to most learning algorithms, which can only work if a fixed network structure is first specified, the orthogonal least squares algorithm is a structural identification technique, where the centres and estimates of the corresponding weights can be simultaneously determined in a very efficient manner during learning. Orthogonal least squares learning procedure generally produces an RBF network smaller than a randomly selected RBF network [3]. Due to its linear computational procedure at the output layer, the RBFN is faster in training time compared to its BP counterpart. A major drawback of this method is associated with the input space dimensionality. For large numbers of input units, the number of radial basis functions required can become excessive. If too many centres are used, the large number of parameters available in the regression procedure will cause the network to be oversensitive to the details of the particular training set and result in poor generalization performance (overfit). Avoid

this problem, both the forward selection and zero-order regularization techniques are proposed and applied in [3] to construct parsimonious RBFN with improved generalization properties.

A RBF network with m outputs and nh hidden nodes can be expressed as:

$$y_i(t) = w_{i0} + \sum_{j=1}^{nh} w_{ij} \phi(|v(t) - C_j(t)|)$$

Where $i=1, \dots, m$.

where w_{ij} , w_{i0} and $c_j(t)$ are the connection weights, bias connection weights and RBF centres respectively, $v(t)$ is the input vector to the RBF network composed of lagged input, lagged output and lagged prediction error and $f(\cdot)$ is a non-linear basis function. (\cdot) denotes a distance measure that is normally taken to be the Euclidean norm. [18] Since neural networks are highly non-linear, even a linear system has to be approximated using the non-linear neural network model. However, modelling a linear system using a non-linear model can never be better than using a linear model. Considering this argument, the RBF network with additional linear input connections is used. The proposed network allows the network inputs to be connected directly to the output node via weighted connections to form a linear model in parallel with the non-linear standard RBF model. The new RBF network with m outputs, n inputs, nh hidden nodes and nl linear input

$$y_i(t) = w_{i0} + \sum_{k=1}^{nl} \alpha_k v_k(t) + \sum_{j=1}^{nh} w_{ij} \phi(|v(t) - C_j(t)|)$$

where the α 's and v_k 's are the weights and the input vector for the linear connections respectively. The input vector for the linear connections may consist of past inputs, outputs and noise lags. Since it appears to be linear within the network, the α 's can be estimated using the same algorithm as for the w 's.

III. INTERVAL SYSTEMS

Moore defined interval arithmetic for rational functions composed of a finite number of the four basic arithmetic operations on intervals of finite real numbers. [11,12,] Corresponding to the situation with real numbers, operations on intervals with extended (including infinite) endpoints and division by intervals containing zero were not defined. [19,20] Originally, neither was raising an interval to an integer power. Since the original formulation, the integer and real power functions have been given interval extensions, but only for intervals contained within function's natural domain of definition. The sets of values that finite interval operations are defined to contain are described as follows:

Let $[a, b]$ denote a real, closed, compact interval constant.

That is, for example:

$$[a, b] = \{x \in \mathbb{R} \mid a \leq x \leq b\}, (1)$$

where \mathbb{R} , denotes the set of finite real numbers, $\{x \mid -\infty < x < +\infty\}$. If $\text{op} \in \{+, -, \times, \div\}$ denotes one of the four basic arithmetic operators (BAOs), where $d < 0$ or $0 < c$ in the case of division, because division by zero is not defined for real numbers. The right-hand side of (2) defines the sets of values that interval arithmetic operations on finite real intervals must contain. While computing narrow intervals is desirable, the only requirement is containment. The right-hand side of (2) is the set of values that the operation, $[a, b] \text{ op} [c, d]$ must contain. The term containment set is used to refer to the set of values that an interval result must contain.

Arithmetic operation monotonicity makes possible the following rules to compute endpoints of finite interval arithmetic operations:

$$\begin{aligned} [a, b] + [c, d] &= [a + c, b + d] \quad (3a) \\ [a, b] - [c, d] &= [a - d, b - c] \quad (3b) \\ [a, b] \times [c, d] &= [\min(a \times c, a \times d, b \times c, b \times d), \\ &\max(a \times c, a \times d, b \times c, b \times d)] \quad (3c) \\ [a, b] \div [c, d] &= [\min(a \div c, a \div d, b \div c, b \div d), \\ &\max(a \div c, a \div d, b \div c, b \div d)] \quad (3d) \end{aligned}$$

where, to exclude division by intervals containing zero, $d < 0$ or $0 < c$. Directed rounding is used to guarantee containment when interval operations are implemented using IEEE-754 floating-point operations. [4,5] Dependence even where there forms no rounding error, this may result in intervals that no way can be treated as requirement. Therefore, it is not surprising if a nominally positive interval near zero contains negative values. [16,17] Subsequently, if a nominally non-negative interval result contains negative values and is an argument of an operation or function with a non-negative domain, existing unclosed interval systems will raise an exception. For example, consider the function $f(x) = x(x - 1) + 1$, (4) evaluated over the interval $X = [-2, 2]$ using interval arithmetic, the value of $X(X - 1) + 1$ is $[-5, 7]$. No rounding errors have been made. Every arithmetic operation is exact. The above result is an example of the dependence problem in interval arithmetic. The expression $X(X - 1) + 1$ is evaluated as if it were instead, $X(Y - 1) + 1$, with the intervals, X and Y , just by coincidence having the same value. To connote the fact that the interval variables X and Y are not identical, but that 2 arithmetic operations on a pair of intervals, $[a, b]$ and $[c, d]$ must produce a new interval, say $[e, f]$, such that $[e, f] \supseteq \{x \text{ op } y \mid x \in [a, b] \text{ and } y \in [c, d]\}$, As long as interval expressions are defined in terms of real or extended-real operations and functions, no escape exists from limitations on the domain of operations and functions in the underlying point systems.

These limitations take two forms: In the real and extended real systems (hereafter point systems), functions are undefined outside their domain of definition. In point systems, a function maps points from its domain to points in its range. [12] Multi-valued relations are mappings of sets of points in the relation's domain set onto sets of points in its range set. Intervals are compact sets of points. This permits the underlying system from which interval arithmetic is derived to also be sets, not single points. The closed centred based set as a system is

defined, which gives the possibility of constructing the closed interval system. This tries to produce enclosures of sets in this or other possible closed centred based set systems. The "Simple" closed interval system, is implemented in the most significant practical consequence of programming with a closed interval system is that without exception. The valid interval result is obtained through the interval operation and an intrinsic function, along with its interval operands. In a closed interval system have no "exceptional events" with which to contend. This result is not limited to a subset of intrinsic functions or operations and functions.

System constructs that either accept or produce REAL type data items have exception-free interval versions. Therefore, without exception, any interval expression can be evaluated if it can be written as a code list, whether it is a function or a relation. The returned interval is guaranteed to be an enclosure of the set of all possible values of the expression over the argument intervals, irrespective of whether the code list includes branches, loops and subprogram calls, array references, or overwriting of a variable's value by a new value. The set of all possible expression values is the containment set of an expression and is proved in, to be the topological closure of the expression.

Interval systems have a number of advantages over the additional real number-based interval system. Two new items are worthy of the attention by closed interval systems algorithm developers are: 1. how to derive containment sets of expressions both at singular points and at arguments that create indeterminate forms and 2. How to verify expression continuity when required.

This Interval arithmetic

The addition, subtraction and multiplication of two intervals $[a,b]$ and $[c,d]$ are respectively defined as

Addition: $[a,b]+[c,d]=[a+b,c+d]$

Subtraction: $[a,b]-[c,d]=[a-b,b-c]$

Multiplication: $[a,b][c,d] = [\min(ac,ad,bc,bd), \max(ac,ad,bc,bd)]$

This possibility of the interval values evaluated through these systems can enhance our output result of RBFNN such that the ratio of comparison factor for prediction can increase its measure of equality in terms of similarity check. Number neurons in the hidden layer also influences the performance of RBF NN. But with too many nodes it will take a longer time to train and some times over fit to data even though we go along with interval systems.

IV. CONCLUSION

The advantage of RBF neural network is that it can be trained much faster than MLP neural network. It can also give a better performance with minimum number of training data set to perform the successful training and this performance can greatly be influenced by taking the linear data set and as well

the non linear data set in the form of interval systems values of evaluating their activation function and the hidden layer input values. Future objective can be testing the system with a standard database, to compare with other training algorithms. This approach of successful study of rbfn through interval systems may drives towards the better prediction works.

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